

# The influence of Lorentz Violation on UHE photon detection

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on behalf on Grigory Rubtsov and Sergey Sibiryakov



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## Based on

- Grigory Rubtsov, Petr Satunin, and Sergey Sibiryakov. "Calculation of cross sections in Lorentz-violating theories". Phys. Rev. D 86, 085012 (2012)
- Petr Satunin. "Width of photon decay in a magnetic field: Elementary semiclassical derivation and sensitivity to Lorentz violation". Phys. Rev. D 87, 105015 (2013)
- Grigory Rubtsov, Petr Satunin, and Sergey Sibiryakov. Constraining Lorentz Violation using possible UHE photon detection. arXiv:1306.xxxx

# Lorentz Invariance Violation

## Motivation

- Several approaches to quantum gravity predict Lorentz invariance violation (LV) at high energies (e.g. Horava-Lifshitz).

*Horava, 2009*

*Blas, Pujolas, Sibiryakov, 2010*

*Kostelecky, Samuel, 1989*

- Theories with violation of the Lorentz Symmetry as an effective theory

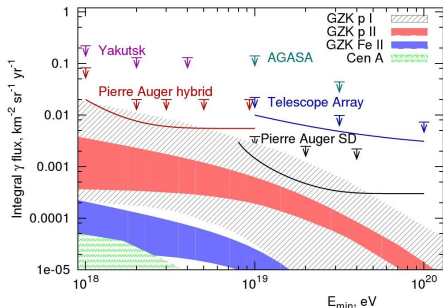
*Kostelecky, Colladay, 1998*

*Coleman, Glashow, 1999*

- Low-energy LV is strictly bounded *Data tables — Kostelecky, Russell, 2011*
- Weaker bounds on high-energy LV — the largest sensitivity in cosmic rays

# UHE photons

- Energies  $10^{18} - 10^{20}$  eV
- Not detected yet
- If reach the Earth, can be detected by surface detectors (Auger, TA)
- Possible sources:
  - Products of GZK process (if protons)  
 $p \gamma_{CMB} \rightarrow p \pi^0$  or  $p \gamma_{CMB} \rightarrow n \pi^+$ ;  $\pi^0 \rightarrow \gamma\gamma$



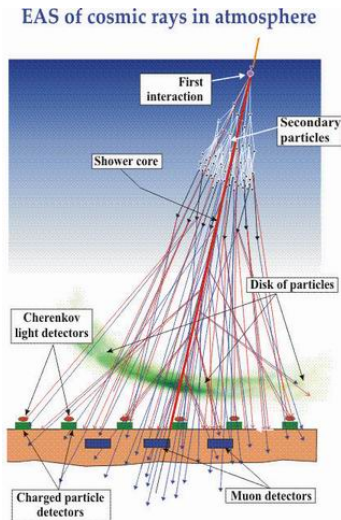
- Exotics (Superheavy DM decay, Z-burst)

# UHE photons detection

## 1st interaction:

$E_{ph} \leq 10^{19.5}$  eV — pair production on Coulomb field of a nuclei  $\gamma N \rightarrow Ne^+e^-$ .  
Atmosphere shower started at  $\sim 10$  km.

$E_{ph} \geq 10^{19.5}$  eV (depend on an angle) — pair production in geomagnetic field  $\gamma \rightarrow e^+e^-$ .  
Small 'preshower' at  $\sim 10^3$  km; subsequent shower in the atmosphere.



# Photon showers. Sensitivity to LV

## Questions:

- Can we detect photon showers in the world without LV?
- What bounds we can establish if UHE photons be detected?

Consider LV, modifying dispersion.

## 3 possibilities:

- Photon decay. No UHE photons in CR. **No showers**  
*Coleman, Glashow '98 ...*
- Suppressed first interaction. Photons but **no showers** due to non-interaction
- LI-like **showers**. Tiny LV or fine-tuning

# Model

- It's complicated to use full SME with nonminimal QED sector in calculations
- Assumptions:  $C$ ,  $P$  and  $T$  unbroken, rotational symmetry in preferred (CMB) frame conserved, LV operators of dim. 4 and 6.
- Inspired by Horava-Lifshitz gravity

$$\mathcal{L} = \bar{\psi} (i\gamma^\mu D_\mu - m) \psi - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\kappa \bar{\psi} \gamma^i D_i \psi + \frac{ig}{M^2} D_j \bar{\psi} \gamma^i D_i D_j \psi + \frac{\xi}{4M^2} F_{kj} \partial_i^2 F^{kj}$$

⇓

Dispersion relations:

$$E_\gamma^2 = k^2 + \frac{\xi k^4}{M^2}, \quad E_e^2 = m^2 + p^2 (1 + 2\kappa) + \frac{2gp^4}{M^2}.$$

Feynman rules modification

see

*Rubtsov, P.S., Sibiryakov, 2012*

# Pair production on a nuclei $\gamma N \mapsto e^+e^-N$



$$\omega_{LV} = -\varkappa k + \left(\frac{\xi}{2} - g\right) \frac{k^3}{M^2}, \quad k \gg m$$

$$k |\omega_{LV}| \ll m^2 \quad \longrightarrow \quad \sigma = \frac{28}{9} \frac{Z^2 \alpha^3}{m^2} \ln \frac{2k}{m} \quad \text{Bethe, Heitler, 1934}$$

$$k |\omega_{LV}| \gg \frac{m^2}{\alpha^2 Z^{2/3}} \quad \longrightarrow \quad \sigma = \frac{4Z^2 \alpha^3}{3} \frac{1}{k |\omega_{LV}|} \left( \ln \frac{k |\omega_{LV}|}{m^2} \right)^2$$

$$m^2 \ll k |\omega_{LV}| \ll \frac{m^2}{\alpha^2 Z^{2/3}} \quad \longrightarrow \quad \sigma = \frac{8Z^2 \alpha^3}{3} \frac{1}{k |\omega_{LV}|} \ln \frac{2k |\omega_{LV}|}{m^2} \ln \frac{1}{\alpha Z^{1/3}}$$

- Suppression  $\sigma_{LV} \sim \sigma_{LI} \cdot \frac{m^2}{k |\omega_{LV}|}$



## Photons showers. Numerical simulations

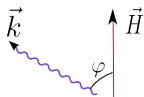
- Simulate  $N < 6$  photon events in agreement with LI hypothesis
- Compare these events with expected signal for LV (KS test)
- Exclude LV parameters

N	95% CL			99% CL		
	$X_{max}, \frac{g}{cm^2}$	$\frac{\sigma^{LI}}{\sigma^{LV}}$	$-\omega_{LV}, 10^{-7} eV$	$X_{max}, \frac{g}{cm^2}$	$\frac{\sigma^{LI}}{\sigma^{LV}}$	$-\omega_{LV}, 10^{-7} eV$
1	-	-	-	-	-	-
2	1 880	18.6	16.76	-	-	-
3	1 380	8.6	5.79	1 970	20.4	18.91
4	1 270	6.4	3.69	1 600	13.0	10.38
5	1 225	5.5	2.88	1 490	10.8	8.03

**Table:** Exclusion bounds on  $X_{max}$  (maximal depth of a shower) and  $\omega_{LV}$  on 95% and 99% CL if  $N$   $10^{19}$  eV photons are detected.

- Bound on positive  $\omega_{LV} \lesssim \frac{2m^2}{k}$  from photon decay (see Galaverni, Sigl '08 other notations)

# Photon decay in magnetic field



$$\vec{H} = (H, 0, 0)$$

$$\vec{k} = (k \cos \varphi, k \sin \varphi, 0)$$

Semiclassical 'Worldline instanton' method

*Affleck, Alvarez, Manton, 1982*

$$\Gamma \propto \int_{p.b.c} Dx_\mu e^{-S[x_\mu]}$$

Semiclassics  $\leftrightarrow$  saddle point approximation

$$LI \quad \leftrightarrow \quad \Gamma \propto \exp \left[ -\frac{8m^3}{3keH \sin \varphi} \right].$$

$$LV \quad \leftrightarrow \quad \Gamma \propto \exp \left[ -\frac{8m^3}{3keH \sin \varphi} \left( 1 - \frac{k \cdot \omega_{LV}}{2m^2} \right)^{3/2} \right].$$

- UHE photon registered with preshower signature  $\rightarrow |\omega_{LV}| < \frac{2m^2}{k}$

## Bounds IF UHE photons be detected

Excellent bounds on some LV parameters...

$\omega$	$10^{19}$ eV	$10^{20}$ eV	current
$ \omega_{LV} $ , eV	$10^{-6}$	$10^{-8}$	-
$ \varkappa  \sim  c_{ii} $	$10^{-26}$	$10^{-28}$	$10^{-17}$
$M_{QG}^{(2)}$ , GeV	$10^{24}$	$10^{25}$	$10^{16}$

... only if photons with energy  $\omega$  be detected.

- but NO evidence for LV in the opposite case

# Conclusions

- Even small LV strongly suppresses pair production (both in an electric field of a nuclei or in a weak magnetic field).
- Possible UHE photon detection can establish very strong two-sided bound on generic type of LV parameters
- **Independent** of any astrophysical model: UHE photon origin does not matter
- These calculations in more general model are complicated but possible..

Thank you for your attention